

***Simulations of
Relativistic Jet Formation
In Radio Sources***

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Talk Outline

- Introduction: observed Lorentz factors
- Review of steady state simulations
- Pseudo-relativistic simulations and the “magnetic switch”
- General relativistic jet production and rotating black holes
- Possible scenarios for Active Galactic Nuclei

Acknowledgements

- Collaborators
 - General Relativistic simulations: S. Koide (Toyama University), K. Shibata, T. Kudoh (National Astron. Obs, Japan)
 - Pseudo-relativistic simulations: D. Payne (Intel), K. Lind (Silicon Graphics), S. Edgington (Caltech), P. Godon (Space Telescope)

Observed Lorentz Factors

- Component proper motions: $\Gamma \equiv (1-v^2/c^2)^{-1/2} = 5-10$
(NOTE: this may measure a pattern speed only)

- Brightness temperature measurements of Doppler boosting:

$$\Gamma \geq 0.5 T_{B,\text{measured}} / T_{B,\text{rest frame}}$$

- $T_{B,\text{rest frame}} \approx 10^{11}$ K for an equipartition synchrotron plasma
- Some measured brightness temperatures and inferred Lorentz factors:
 - Ground Radio VLBI: $T_{B,\text{measured}} \geq 10^{12}$ K $\Rightarrow \Gamma \geq 5$
 - Space VLBI (VSOP): $T_{B,\text{measured}} \geq 7 \times 10^{12}$ K $\Rightarrow \Gamma \geq 35$
 - Intra-day variable sources: $T_{B,\text{estimated}} \sim 5 \times 10^{14}$ K (?) $\Rightarrow \Gamma \geq 2500$ (?)

The Case for Space VLBI (Part I)

- Measuring brightness temperatures is the best (and possibly only) method for determining the highest velocities nature can achieve
- A measured brightness temperature depends only on the source flux and the length of the baseline
- T_B measured from the ground is limited to $< 10^{12}$ K, regardless of observing frequency
- Higher T_B , and Lorentz factors significantly above 10, can be measured only with baselines much longer than an earth diameter \Rightarrow NEED SPACE VLBI
- VSOP has found unresolved, ~ 1 Jy, high T_B cores in nearly all sources studied (see Lister *et al.*, Piner *et al.* this meeting)
 - \Rightarrow A HIGHLY SENSITIVE SPACE VLBI MISSION WITH LONG BASELINES (*e.g.*, ARISE-LITE, VSOP-2) IS CRUCIAL FOR RESOLVING THESE CORES AND MEASURING THEIR ACTUAL JET SPEEDS

Conclusions

- The magnetically-driven outflow has two main components:
 - A slowly-collimating wind from the surface of the accretion disk
 - A highly-collimated jet from the inner edge of the disk or torus
- Both types of outflow are subject to “magnetic switching”:

There exists a critical MHD power $L_{\text{crit}} \equiv E_{\text{escape}}/\tau_{\text{free-fall}}$ (analogous to the Eddington limit) such that

 - When the MHD power in the rotating magnetic field $L_{\text{MHD}} < L_{\text{crit}}$, gravity is *important*, and the jet/wind speed is limited to $V_{\text{jet}} \sim V_{\text{escape}}$
 - When $L_{\text{MHD}} > L_{\text{crit}}$, gravity is *unimportant*, and the jet/wind speed is determined mainly by the output MHD power and the mass loss:

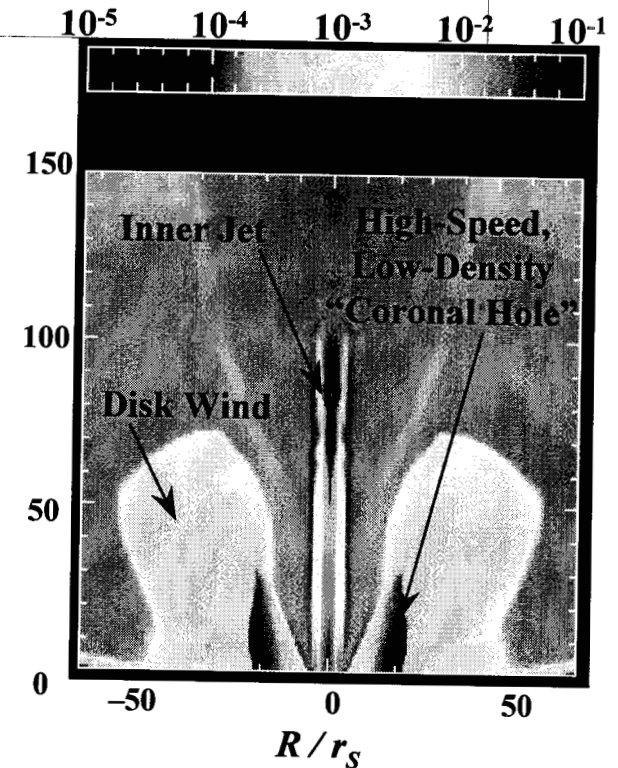
Non-relativistic:

$V_{\text{jet}}^2 \sim L_{\text{MHD}}$

Relativistic:

$\Gamma_{\text{jet}} c^2 \sim L_{\text{MHD}}$
- High MHD power + low mass loss (Poynting-flux-dominated)

\Rightarrow high Lorentz factors

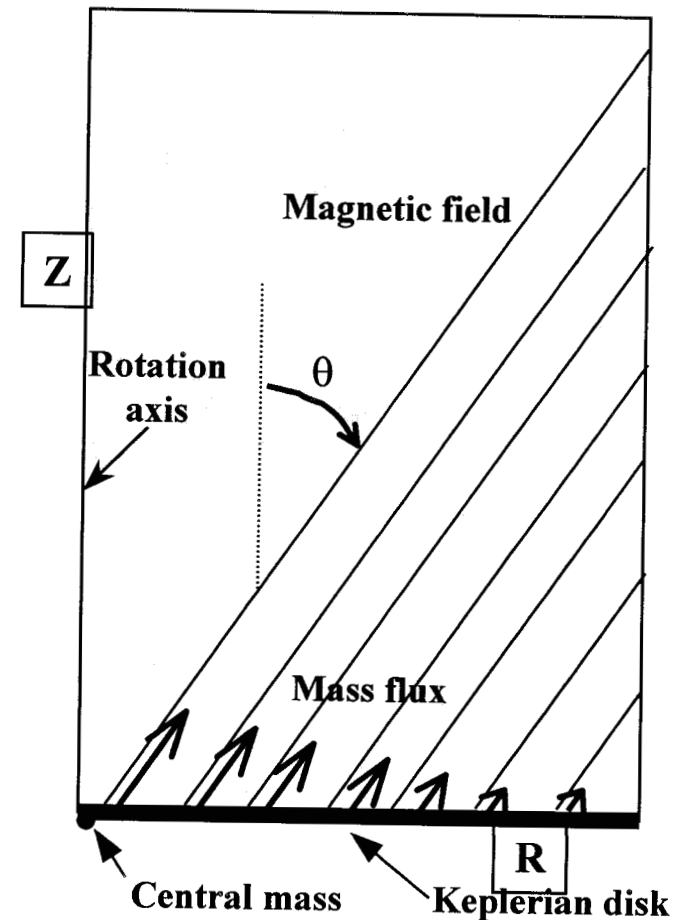


Conclusions (continued)

- When the accreting object is a rotating black hole:
 - The jet is accelerated from the “frame-dragged” accreting matter inside the ergosphere
 - Recall:
 - The horizon is much smaller than one Schwarzschild radius (GM/c^2 for maximal Kerr)
 - All matter in the region $R < 2 GM/c^2$ (the “ergosphere”) must rotate with the black hole
 - The strongest and fastest jets occur when:
 - The black hole is rotating rapidly
 - The accreting material plunges rapidly into the ergosphere
 - *E.g.*, when the accretion is an Advection-Dominated Accretion Flow [ADAF] or
 - *E.g.*, when the accretion disk counter-rotates relative to the black hole

Review of Steady State Simulations

- Some numerical simulations have attempted to reproduce the steady state Blandford & Payne solutions (Ustyugova et al. 1995, 1999; Ouyed et al. 1997; Krasnopolsky et al. 1999)
- Key ingredients in steady-state simulations:
 - An infinitely-thin accretion disk boundary condition, stretching to $R=0$
 - A central mass gravitational potential with a small “smoothing radius”
 - Keplerian rotation
 - Fixed vertical magnetic field B_z
 - Fixed mass flux along the field lines
 - Important: the following quantities on the boundary are allowed to adjust to the steady-state solution: radial B_R and toroidal B_ϕ magnetic field strength, and radial velocity V_R

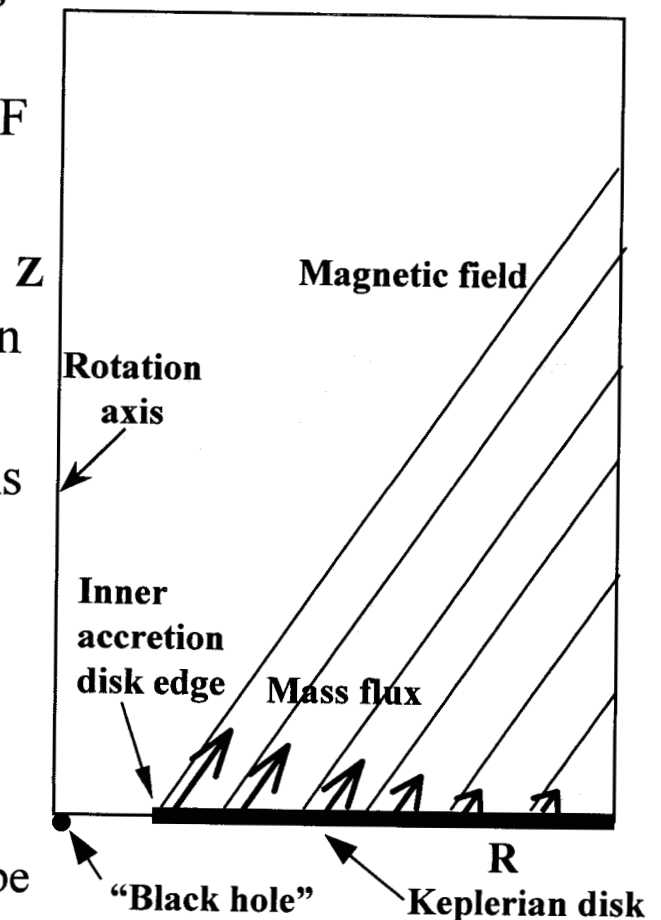


Pseudo-Relativistic Simulations of Black Hole Accretion Disks

- When the disk coronal material is not a relativistic gas ($c_{\text{sound}} < c$; $V_{\text{Alfvén}} < c$), the non-relativistic MHD equations are nearly identical to the relativistic ones, IF we replace the velocity V with the proper velocity U

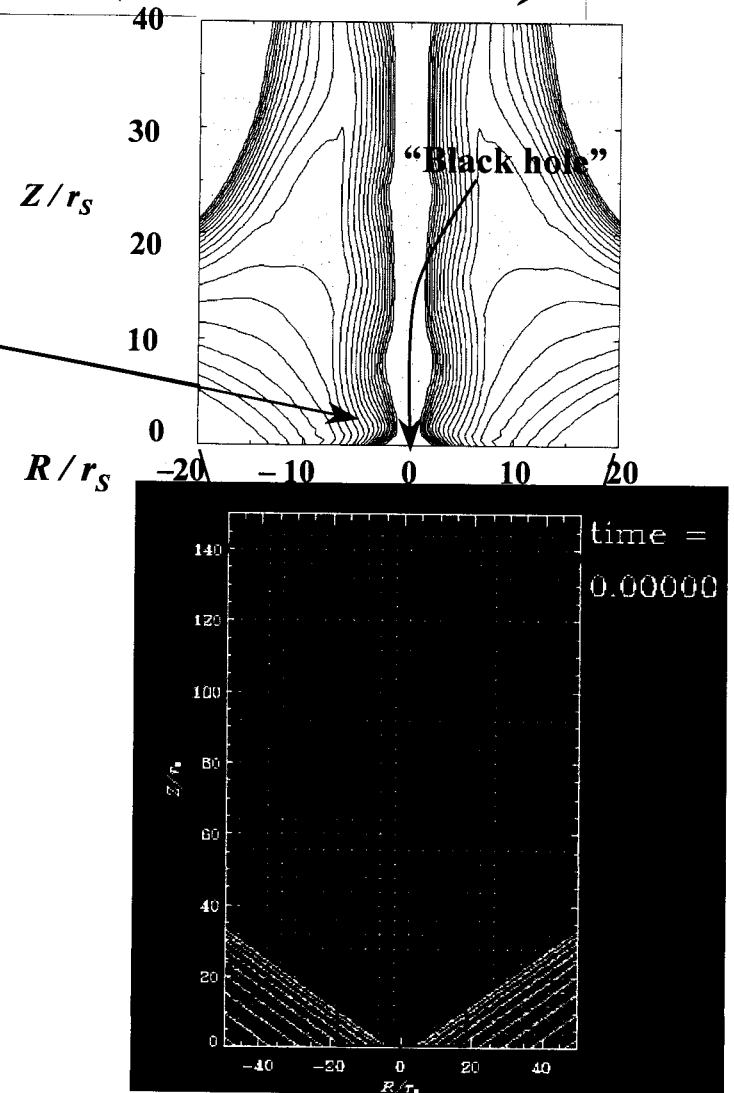
$$V \rightarrow U = \Gamma V$$

- In these simulations, velocities much greater than 1 can be identified with the Lorentz factor Γ
- Key ingredients in these pseudo-relativistic simulations (Lind, Meier, & Payne 1994; Meier *et al.* 1997; Meier *et al.* 2000):
 - Similar to previous “disk as boundary” simulations, but
 - Infinitely-thin accretion disk has an inner radius at $R=6GM/c^2$
 - B_R , B_ϕ , and V_R are all fixed on the boundary (as would be the case in an actual accretion disk)



Pseudo-Relativistic Simulations of Black Hole Accretion Disks (continued)

- Results (Meier et al. 1997; 2000):
 - This inner disk edge and fixed disk field create a new magnetic field structure:
 - Gravitational and magnetic forces cause injected corona to accrete inward, above the disk
 - This bends the magnetic field inward, creating a substantial B_R
 - Differential rotation winds B_R up into B_ϕ , which expels and collimates a narrow jet
 - This inner jet in the accreting corona case is similar to that in the accreting torus case shown by Shibata-san
 - A slowly-collimated disk wind (like the Blandford-Payne solutions) also occurs occasionally, but usually only when the inner jet is weak

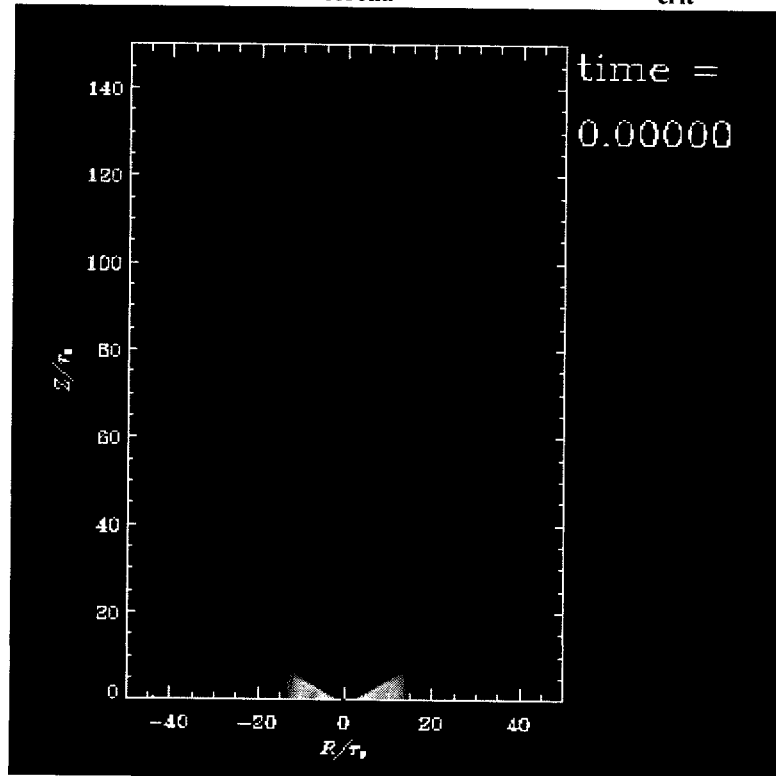


Pseudo-Relativistic Simulations of Black Hole Accretion Disks (continued)

- The “Magnetic Switch” process (Meier *et al.* 1997; Meier 1999):
 - There appears to be a critical MHD luminosity (analogous to the Eddington limit)

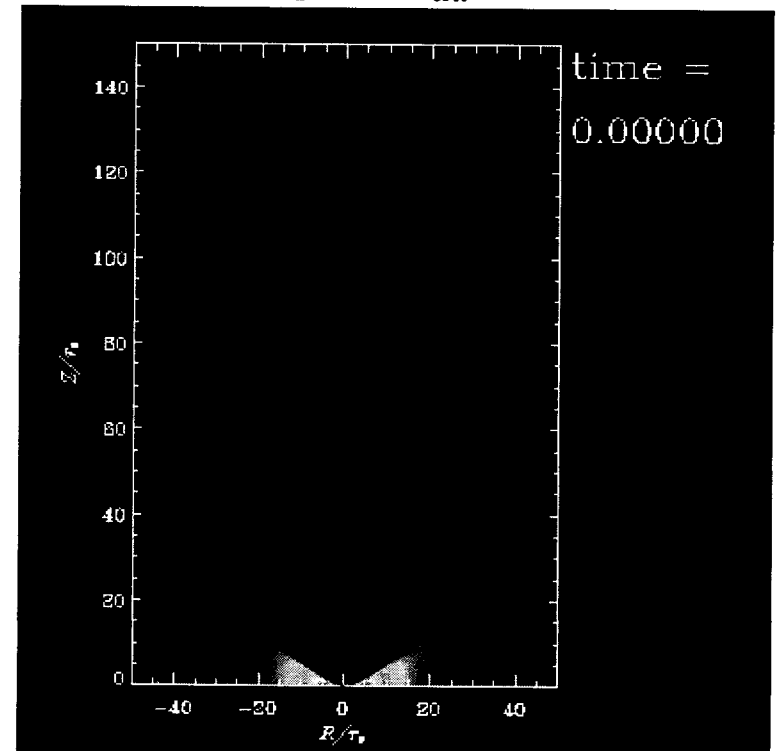
$$L_{\text{crit}} \equiv E_{\text{escape}} / \tau_{\text{free-fall}} = 4 \pi \rho_{\text{corona}} R_{\text{corona}}^2 (G M / R_{\text{corona}})^{3/2}$$

$$L_{\text{MHD}} = B_{\text{corona}}^2 R_{\text{corona}}^4 \Omega^2 / 4c \sim 0.8 L_{\text{crit}}$$



When $L_{\text{MHD}} < L_{\text{crit}}$, $V_{\text{jet}} \sim V_{\text{esc}}$,
resulting in a relatively slow jet

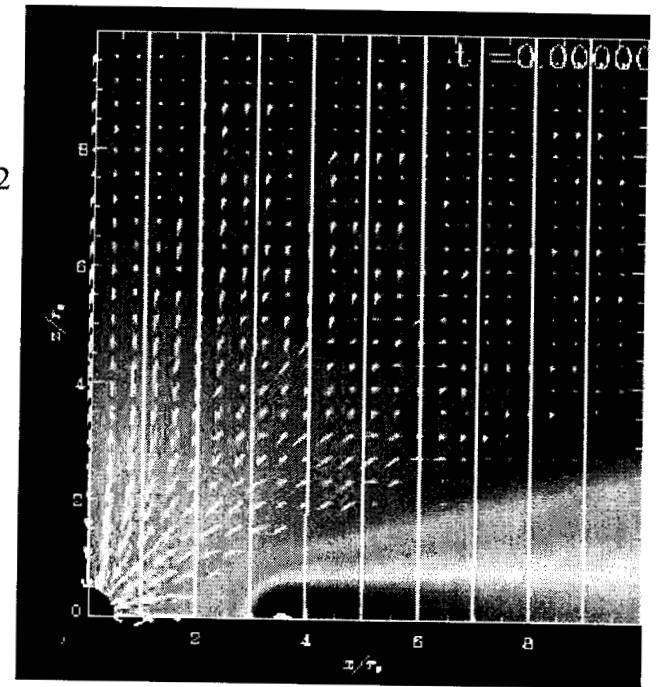
$$L_{\text{MHD}} \sim 1.5 L_{\text{crit}}$$



When $L_{\text{MHD}} > L_{\text{crit}}$, V_{jet} is determined by $L_{\text{MHD}} \sim \Gamma_{\text{jet}} c^2$,
resulting in a relatively fast jet

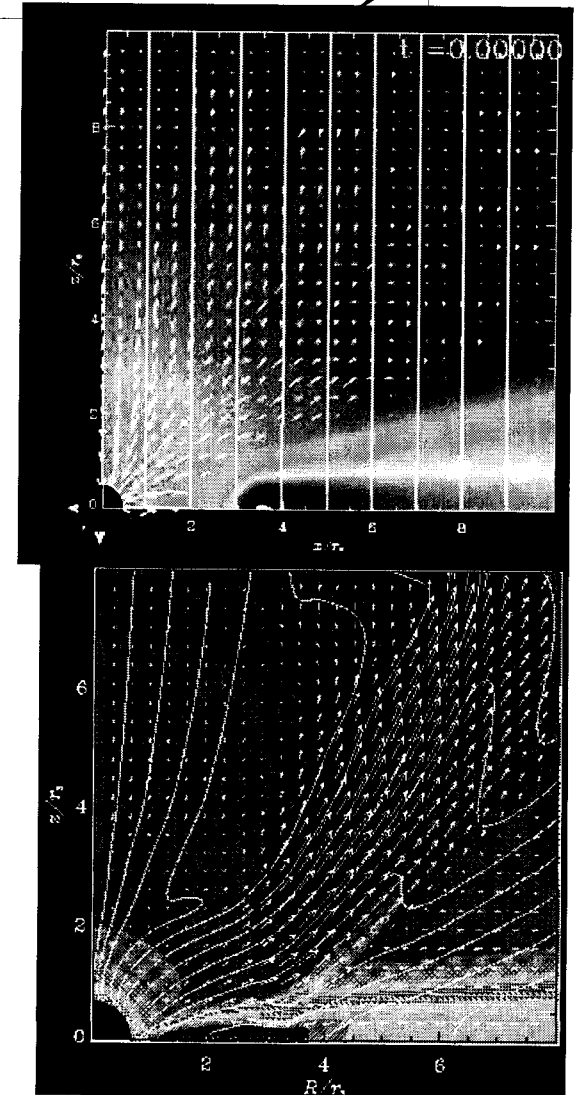
General Relativistic Simulations of Black Hole Accretion Disks

- Main papers: Koide, Shibata, & Kudoh (1998); Koide, Meier, Shibata, & Kudoh (1999a,b)
- Key ingredients:
 - Thick accretion disk with inner edge at $R = 4.5 \text{ GM}/c^2$
 - Initial vertical weak magnetic field ($V_{\text{Alfvén}} = 0.01c$)
 - Fixed general relativistic gravitational potential and fully relativistic MHD flow
- Five scenarios were simulated:
 - Non-rotating (Schwarzschild) black hole, non-rotating (ADAF-like) disk
 - Non-rotating black hole, Keplerian disk
 - Rotating (Kerr) black hole ($a/M=0.95$), non-rotating (ADAF-like) disk
 - Rotating black hole, Keplerian disk
 - Co-rotating with the black hole rotation
 - Counter-rotating against the black hole rotation



General Relativity Simulations of Black Hole Accretion Disks (continued)

- Results for Kerr (rotating) hole, counter-rotating disk:
 - Disk plunges rapidly toward black hole (counter-rotating orbits are unstable!)
 - Dragging of inertial frames by rotating black hole reverses spin of disk
 - A jet is generated from the inner disk edge in a manner similar to non-relativistic simulations
 - A very low density region forms inside the jet --- potentially the beginning of a magnetically-switched, high Lorentz factor flow
- Similar results for Kerr hole, non-rotating disk:
 - Disk free-falls rapidly into ergosphere
 - Rotation of black hole contributes significantly to acceleration of jet
 - Highest jet velocities achieved so far are of order the ergospheric escape velocity: $\Gamma < 3$



General Relativistic Simulations of Black Hole Accretion Disks (continued)

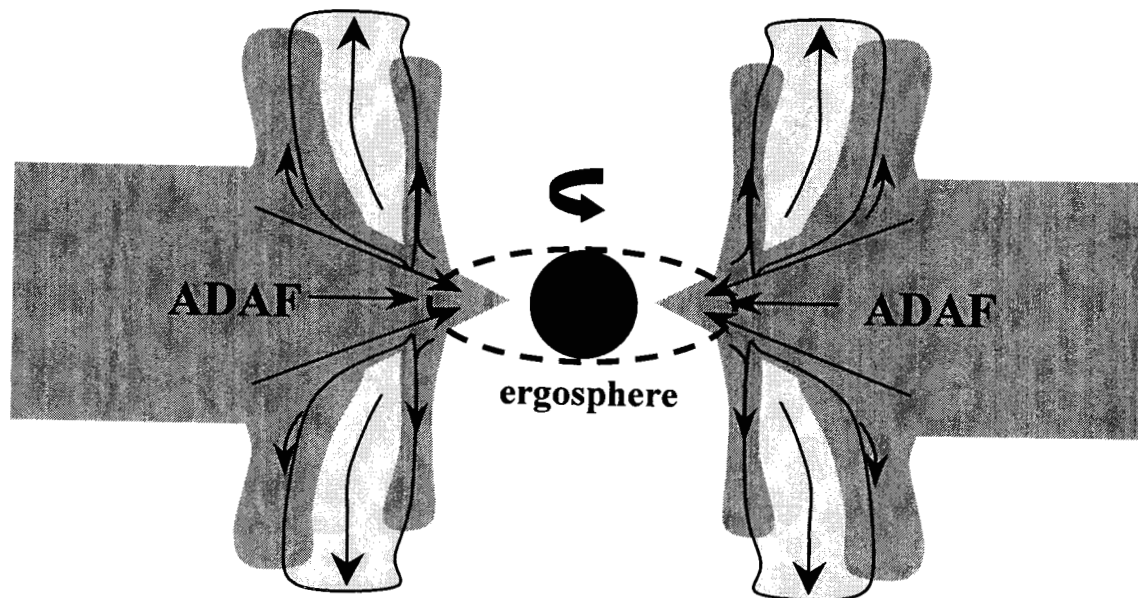
- Results for Kerr hole, co-rotating disk:
 - Disk accretes slowly toward black hole (co-rotating orbits are stable!)
 - Some outflow is produced, but it is rather slow so far ($V_{\text{jet}} \sim 0.4 c$)
 - Further evolution is unclear (simulation had to be stopped for numerical reasons)
- Results for Schwarzschild holes:
 - Jet is produced only when the disk is rotating
 - Jet speed is limited to $V_{\text{jet}} \sim V_{\text{esc}} (R=6GM/c^2) = 0.6 c$
- Summary from all simulations: The fastest and most powerful jets are produced when
 - The central black hole rotates rapidly
 - The accreting material falls rapidly into the ergosphere
 - The material accelerated in the jet is of very low density
(i.e., $L_{\text{MHD}} > L_{\text{crit}}$ or, for Keplerian rotation, $V_{\text{Alfvén}} > V_{\text{esc}}$)

Summary of All Simulations Performed

- The fastest and most powerful jets are produced when
 - The central black hole rotates rapidly
 - The accreting material falls rapidly into the ergosphere
 - The material accelerated in the jet is of very low density
(*i.e.*, $L_{\text{MHD}} > L_{\text{crit}}$ or, for Keplerian rotation, $V_{\text{Alfvén}} > V_{\text{esc}}$)

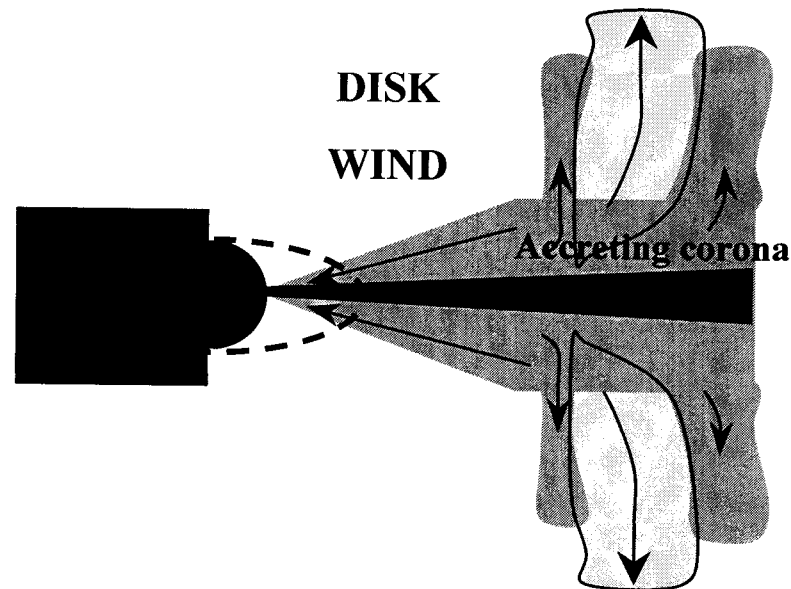
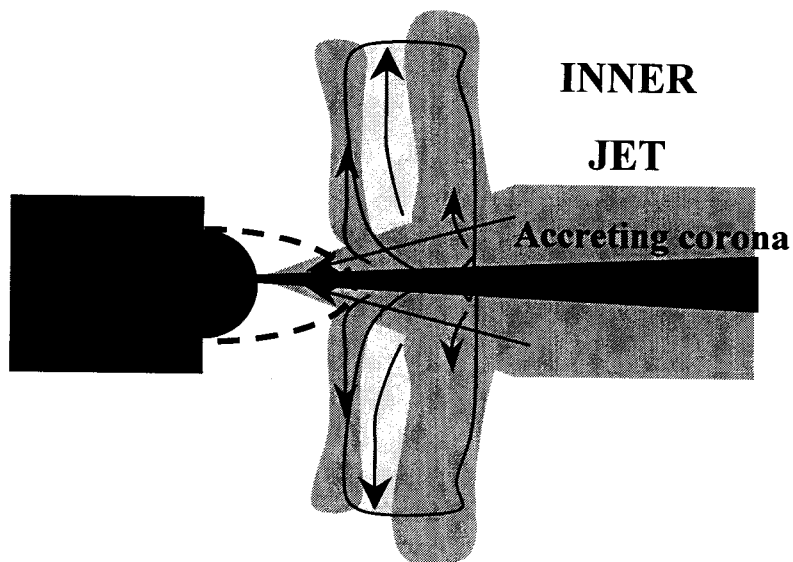
Two Possible Scenarios for AGN

- Scenario #1: Advection-Dominated Accretion Flow into Rotating Black Hole
 - Rapid infall toward black hole
 - Little rotation in the accretion flow until it plunges into the ergosphere
 - Jet is produced and collimated very near the black hole
 - Much of the outflow is at the escape velocity ($\Gamma < 3$)
 - Highest Lorentz-factor flow ($\Gamma \gg 10$) can occur in low-density, Poynting-flux-dominated, “coronal holes”



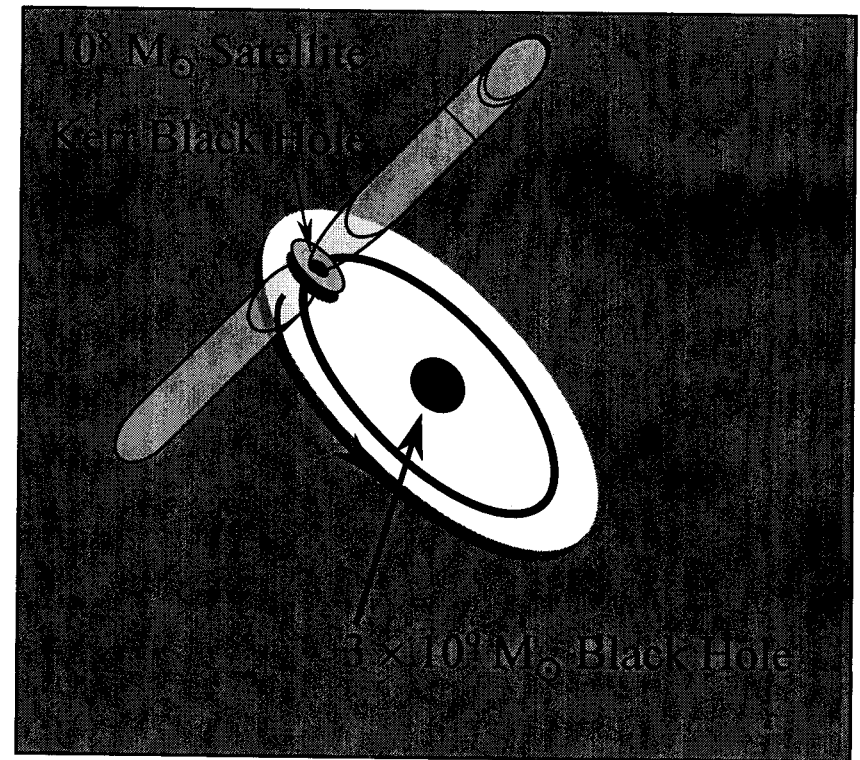
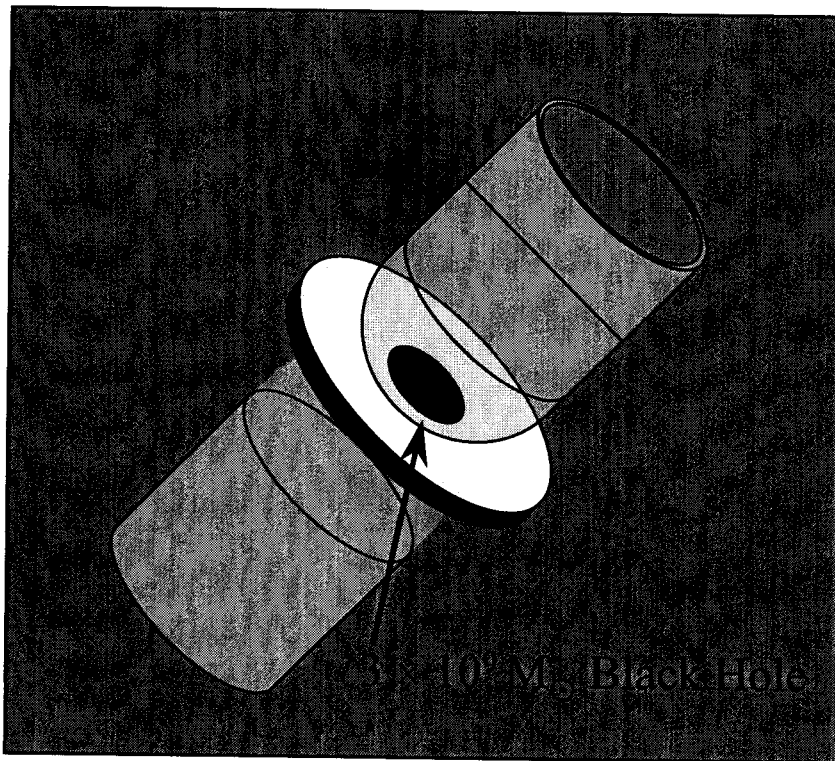
Two Possible Scenarios for AGN (continued)

- Scenario #2: Advection-Dominated Coronal Accretion Flow
 - Magnetic field is anchored in thin Keplerian-rotating accretion disk
 - Rotating disk can accelerate inner jet or outer wind
 - Again, much of the outflow is at the escape velocity ($\Gamma < 3$)
 - But, high Lorentz-factor flow ($\Gamma \gg 10$) can occur in low-density, Poynting-flux-dominated, “coronal holes”
 - Jet can be collimated far from the black hole and still have a high Lorentz factor (*cf.* M87)



Two Possible Models for M87: The Case for Space VLBI (Part II)

- Model #1: broad relativistic wind from accretion disk, collimating into a highly-relativistic jet
- Model #2: satellite rotating black hole with highly-collimated, relativistic inner jet



⇒ A SENSITIVE SPACE VLBI MISSION WITH 22 and 43 GHz IMAGING
WILL BE ABLE TO DISTINGUISH BETWEEN THESE TWO MODELS

The Future

- General relativistic MHD simulations
 - Improve GRMHD code to handle very low-density flows
 - Investigate magnetic switching in fully-relativistic, finite-thickness accretion disk situations
- Accretion disk structure calculations
 - Investigate the structure of a rotating black hole magnetosphere and its implications for MHD-driven outflow